Package: RFQT (via r-universe)

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 $\mathbf{Type} \ \mathbf{Package}$

Title Random Forest of Q Trees Version 0.1.0 Author Haodong Tian Maintainer Haodong Tian <haodong.tian@mrc-bsu.cam.ac.uk> Description Data-adaptive method for effect heterogeneity analysis or non-linear causal studies in Mendelian randomization and instrumental variables analysis. License GPL (≥ 2) Encoding UTF-8 LazyData true Imports stats, MendelianRandomization, tidyverse, data.table, parallel Suggests dplyr Repository https://mrcieu.r-universe.dev RemoteUrl https://github.com/HDTian/RFQT RemoteRef HEAD $\mathbf{RemoteSha} \ 1 edae 49a2 fcba3d1 f64db12c1149947d1805469 a$

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BootstrapTreeFitting One Bootstrap Q Tree Fitting

Description

BootstrapTreeFitting fits the Q-tree for a bootstrap data of the training set (with user-specific seed) and store the cleaned results. If you do not need results but the original (dirty) Q-tree information, you may use GetTree().

Usage

```
BootstrapTreeFitting(seed=1,
```

```
Odat=odat,
Vdat=vdat,
honest=FALSE,
S=5,
rate=0.4,
SingleM=FALSE,
Qthreshold=3.84,
method='DR',
SoP=10,
howGX='SpecificGX',
Halve=FALSE,
endsize=1000,
const=NA)
```

Arguments

seed	seed value for reproducible and traceable results
Odat	a data frame. This is recognized as the training data set.
Vdat	a data frame. This is recognized as the testing or validation data set.
honest	Logical value indicates whether to use the honest estimation style or not. Default value is ${\tt FALSE}.$ When honest estimation is used, the tree construction and the leaf-specific estimates will be obtained in two separate samples of the (boostrapped) training data.
S	a postive integer indicates the maximum tree depth allowed. Default value is 5 (i.e. the data set is allowed to be splitted at most 5 times). S is also conneted to the argument <code>endsize</code> , both of which work in a similar way. One may only restrict one of them and leave another one be a flexible value (e.g. S=100 or <code>endsize=0</code>).
rate	a value ranging from 0 to 1 indicates the proportion of the candidate covariates to be randomly cosidered in each split when construcing the Q-tree.
SingleM	Logical value indicates whether to use one single covariate variable at all times. Default value is FALSE. If SingleM=TRUE, the covariate used are the best variable indicated by GetIndex.

Qthreshold	A positive value used as the threshold value for the Q statistic. Default value is 3.0. One can set Qthreshold=0 to ignore the Q-related stopping rule.
method	a character indicates the stratification method used for constructing a Q-tree. There are currently three methods: the Doubly-ranked method (method='DR'), the residual methods (method='Residual') and the naive method (recognized by any character except 'DR' and 'Residual'). The default method is 'DR'.
SoP	a postive integer $(>=2)$ indicates the size of pre-straum. Only applicable for the doubly-ranked stratification. Default value is 10.
howGX	a character indicates the way to calculate the instrument-exposure associations. Two ways are currenly allowed: the instrument-exposure associations estimated seperately at each stratum (howGX='SpecificGX'), or use a fixed instrument-exposure association (howGX='const')
Halve	Logical. Indictes whether to split the node by half: half (i.e. 5:5). Default value is ${\tt FALSE}.$
endsize	a positive integer value indicates the minimual size of the node of Q-tree. ${\tt S}$ and <code>endsize</code> work in a similar way.
const	a value indicates the fixed instrument-exposure association value used for constructing the Q-tree. Only applicable for $howGX='SpecificGX'$.

Details

The training data Odat and the testing data Vdat should be of the same form and be a data frame that can be regonized by the functions. The first four columns must be the individual IDs, the (one-dimensional) instrument, the exposure (should be NA if not available), and the outcome, respectively. The (high-dimensional) covariates are then following. Note that all the functions may be working with incorrect column ordering, but the results are misleading. Do make sure the column variable order is correct.

If simulated data is used, there should be a end column named as true_STE. That is, odat\$true_STE is not NULL.

If the data does not contain the exposure information, the RFQT can still be fitted, where one should use howGX='const' with a external instrument-exposure association (usually from independent studies).

Value

BootstrapTreeFitting returns a list with the following components:

end_node_inform	mation
	the end nodes (leaves) information of the fitted Q tree, which contains the end-node index, the MR estimates, and the sample size proportion.
OOB_predict	the predicted effects of the OOB samples accrding to the Q-tree. Values will be 0 if the individual is not out of bag.
v_predict	the predicted effects of the testing samples accrding to the Q-tree.

vi1	the vector of the variable importance (VI) measurements for all the can- didate covariates considered.
vi2	the vector of the variable importance (VI) measurements for all the can- didate covariates considered. This VI measurements do not need the individual true effect information, therefore suitable for real application data.
ts1	the value of the permutation test with statistic S1.
ts2	the value of the permutation test with statistic S2.

When the real data is fitted, vi1 is not applicable. When only traning data is available, v_predict is not applicable.

References

Burgess, S., Davies, N. M., & Thompson, S. G. (2014). "Instrumental variable analysis with a nonlinear exposure–outcome relationship". Epidemiology (Cambridge, Mass.), 25(6), 877. (Residual stratification)

Tian, H., Mason, A. M., Liu, C., & Burgess, S. (2023). "Relaxing parametric assumptions for non-linear Mendelian randomization using a doubly-ranked stratification method". PLOS Genetics, 19(6), e1010823. (Doubly-ranked stratification)

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
odat<-res$traning.set #training set</pre>
vdat<-res$testing.set #testing set
#When running RFQT with mutiple Q trees/bootstrap - use parallel computation
Nb<-5 #how many trees in the forest? e.g. 5 trees
cl<-makeCluster(2)# clusters/</pre>
clusterEvalQ(cl=cl , expr=library(dplyr))
clusterEvalQ(cl=cl , expr=library(MendelianRandomization) )
clusterExport( cl=cl , varlist=c( 'odat', 'vdat',
                                     'GetTree', 'GetNindex', 'GetIndex' ) )#or any other arguments
                 cl , 1:Nb, BootstrapTreeFitting )
RES<-parSapply(
stopCluster(cl)
dim(RES)#7 Nb
##If you wish to use your own parameters rather than the default parameters, try:
#general exmaple
user_BootstrapTreeFitting<-function(seed){</pre>
  RES<-BootstrapTreeFitting(seed,
                            honest=my.honest,
                            S=my.S,
```

```
JJ=my.JJ,
                                         #or any partial of the arguments
                            rate=my.rate,
                            Qthreshold=my.Qthreshold,
                            method=my.method,
                            SoP=my.SoP,
                            howGX=my.howGX,
                            endsize=my.endsize)
 return(RES)
}
#specific exmaple
user_BootstrapTreeFitting<-function(seed){</pre>
 RES<-BootstrapTreeFitting(seed,SoP=20)
 return(RES)
}
###parallel computation -> RFQT
Nb<-5 #how many trees in the forest?
cl<-makeCluster(2)</pre>
clusterEvalQ(cl=cl , expr=library(dplyr))
clusterEvalQ(cl=cl , expr=library(MendelianRandomization) )
clusterExport( cl=cl , varlist=c( 'odat', 'vdat',
                                     'GetTree', 'GetNindex', 'GetIndex', 'BootstrapTreeFitting') )
RES<-parSapply(
                  cl , 1:Nb, user_BootstrapTreeFitting )
stopCluster(cl)
```

```
DTfit
```

Fit a Classical Single Decision Tree (DT)

Description

DTfit fits a data set (the training data) by the classical Q tree, and return the summary results. DTfit works similarly as GetTree and BootstrapTreeFitting, but not designed or used for future random forest fitting. If you wish to fit data via single tree rather than random forest, use DTfit.

Usage

```
DTfit(Odat = odat,
    Vdat = NA,
    honest = FALSE,
    S = 5,
    rate =1,
    SingleM = FALSE,
    Qthreshold = 3.84,
    method = "DR",
    SoP = 10,
    howGX = "SpecificGX",
    Halve = FALSE,
    endsize = 1000,
    const = NA)
```

Arguments

Odat	a data frame. This is recognized as the trainging data set.
Vdat	a data frame. This is recognized as the testing or validation data set. The default value is NA , indicating that no testing data will be considered.
honest	logical value indicates whether to use the honest estimation style or not. Default value is FALSE. When honest estimation is used, the tree construction and the leaf-specific estimates will be obtained in two seperate samples of the (boostrapped) training data.
S	a postive integer indicates the maximum tree depth allowed. Default value is 5 (i.e. the data set is allowed to be splitted at most 5 times). S is also conneted to the argument endsize, both of which work in a similar way. One may only restrict one of them and leave another one be a flexible value (e.g. $S=100$ or endsize=0).
rate	a value ranging from 0 to 1 indicates the proportion of the candidate covariates to be randomly cosidered in each split when construcing the Q-tree.
SingleM	logical value indicates whether to use one single covariate variable at all times. Default value is FALSE. If SingleM=TRUE, the covariate used are the best variable indicated by GetIndex.
Qthreshold	a positive value used as the threshold value for the Q statistic. Default value is 3.84. One can set Qthreshold=0 to ignore the Q-related stopping rule.
method	a character indicates the stratification method used for constructing a Q-tree. There are currently three methods: the Doubly-ranked method (method='DR'), the residual methods (method='Residual') and the naive method (recognized by any character except 'DR' and 'Residual'). The default method is 'DR'.
SoP	a postive integer $(>=2)$ indicates the size of pre-straum. Only applicable for the doubly-ranked stratification. Default value is 10.
howGX	a character indicates the way to calculate the instrument-exposure associations. Two ways are currenly allowed: the instrument-exposure associations estimated seperately at each stratum (howGX='SpecificGX'), or use a fixed instrument-exposure association (howGX='const').
Halve	logical. Indictes whether to split the node by half: half (i.e. 5:5). Default value is ${\tt FALSE}.$
endsize	a positive integer value indicates the minimual size of the node of Q-tree. S and $\tt endsize$ work in a similar way.
const	a value indicates the fixed instrument-exposure association value used for constructing the Q-tree. Only applicable for $howGX='SpecificGX'$.

Details

Like <code>RFQTfit</code>, <code>DTfit</code> is an integrated function combining other functions, including <code>getPredict</code> and <code>getVI</code>.

DT fit

The training data Odat and the testing data Vdat should be of the same form and be a data frame that can be regonized by the functions. The first four columns must be the individual IDs, the (one-dimensional) instrument, the exposure (should be NA if not available), and the outcome, respectively. The (high-dimensional) covariates are then following. Note that all the functions may be working with incorrect column ordering, but the results are misleading. DO make sure the column variable order is correct.

Value

DTfit returns a list consisting of the following components:

end_node_information

	the end nodes (leaves) information of the fitted Q tree, which contains the end-node index, the MR estimates, and the sample size proportion.
v_predicted	the predicted effects of the testing samples accrding to the Q-tree.
ts1	the value of the permutation test with statistic S1.
ts2	the value of the permutation test with statistic S2.
MSE	the MSE results for the testing samples (if both of the testing set and the label exist).
rdat	the tree fitted data.

References

Burgess, S., Davies, N. M., & Thompson, S. G. (2014). "Instrumental variable analysis with a nonlinear exposure–outcome relationship". Epidemiology (Cambridge, Mass.), 25(6), 877. (Residual stratification)

Tian, H., Mason, A. M., Liu, C., & Burgess, S. (2023). "Relaxing parametric assumptions for non-linear Mendelian randomization using a doubly-ranked stratification method". PLOS Genetics, 19(6), e1010823. (Doubly-ranked stratification)

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the default setting: scenario='A' and SoM=0.5
odat<-res$traning.set #training set
vdat<-res$testing.set #testing set
DTRES<-DTfit(odat,vdat)
DTRES
#get (testing set) MSE manually
mean( ( DTRES$v_predict - vdat$true_STE )^2 )</pre>
```

getDat

Description

getDat creats a toy data based on a certain model

Usage

```
getDat(N = 150000,
    Nt = 100000,
    Nc = 20,
    scenario='A',
    SoM = 0.5,
    ZXeffect = 0.5,
    Random = TRUE,
    label = TRUE,
    split = TRUE)
```

Arguments

Ν	a integer indicates the total sample size (training data size $+$ testing data size)
Nt	a integer indicates the size of the training data.
Nc	a integer indicates the number of candidate variables.
scenario	a character indicates the model scenarios data will be simulated from. $`A'$ refers to scenario where no colliders. $'B'$ refers to the scenario that half covariates will be colliders. $'C'$ refers to more complicated collider scenarios.
SoM	a value indicates the strength of modification (i.e. how strong will the covariate modify the treatment effect). Note even if $SoM=0$, there still exists weak modification.
ZXeffect	a value indicates the instrument-exposure effect.
Random	logical. Indicates whether to use the random value for strenght modification. Default value is TRUE, where weak modification always exists even if $SoM=0$ due to randomness.
label	logical. Indicates whether to added the final column of the simulated data as the true heterogenerous effect (i.e. label). Default value is TRUE .
split	logical. If ${\tt FALSE},$ only one data set is returened. The default is ${\tt TRUE},$ the data will be splitted into the training data and testing data.

Details

The data-generating model is the same as the Scenarios in the original paper, where the first 5 covariates are the true effect modifiers. The covariates in even positions (2,4,...) are the common downstream variables of the exposure and te confounders, therefore causing collider bias (when conditioning on these variables).

GetIndex

Value

getDat() returns a list with three kings of toy data set

whole.data	the complete whole dataset
traning.set	the training set
testing.set	the testing set
SoM	Strength of Modification
modifier_vec	the modification strength vector for each covariate
Scenario	scenario information

the training set and the testing set are of the same form that can be regonized by all the functions. The first four columns are the individual IDs, the instrument, the exposure, and the outcome, respectively. The high-dimensional (dimensions = Nc) covariates are then following. The end column is true_STE, representing the individual controlled direct treatment effect (see more details in the original paper).

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
odat<-res$traning.set #training set
vdat<-res$testing.set #testing set</pre>
```

GetIndex

Get the Best Covariate Index

Description

GetIndex gives the best covariate index according to the inputed data set. The best covariate is one out of the candidate covariates considered that gives the largest Q statistic value.

Usage

Arguments

dat_current	A data frame. This data frame has the first four columns: individual IDs, the instrument, the expoure, and the outcome with the candidate covariates following.		
JJ	A positive integer indicates the total number of the candiate covariates.		
rate	a value ranging from 0 to 1 indicates the proportion of the candidate covariates to be randomly cosidered in each split when construcing the Q-tree.		
SpecificM	a vector indicates the index of candidate variables that can be considered in spliiting. The default value is NA , which means all candidate variables are possible to be considered.		
method	a character indicates the stratification method used for constructing a Q-tree. There are currently three methods: the Doubly-ranked method (method='DR'), the residual methods (method='Residual') and the naive method (recognized by any character except 'DR' and 'Residual'). The default method is 'DR'.		
SoP	a postive integer $(>=2)$ indicates the size of pre-straum. Only applicable for the doubly-ranked stratification. Default value is 10.		
howGX	a character indicates the way to calculate the instrument-exposure associations. Two ways are currenly allowed: the instrument-exposure associations estimated seperately at each stratum (howGX='SpecificGX'), or use a fixed instrument-exposure association (howGX='const')		
Halve	Logical. Indictes whether to split the node by half: half (i.e. 5:5). Default value is ${\tt FALSE}.$		
const	a value indicates the fixed instrument-exposure association value used for constructing the Q-tree. Only applicable for <code>howGX='SpecificGX'</code> .		

Details

GetIndex helps to decide the splitting covariate at the present node when constructing a Q-tree.

Value

 ${\tt GetIndex}$ returns a vector with the following three values:'Candidate.index', 'Q.value' , 'node.size'

Candidate.index

 The index (position rank) of the chosen covariate.

 Q.value
 The corresponding Q statistic value of the chosen covariate.

 minimal.node.size.after.split

 The mimimal sample size of the sun-nodes after splitting.

 split.style

 Three values denoted by 1,2,3 representing the splitting style used for the final covariate. They are 3:7, 5:5, 7:3, respectively.

getMSE

References

Burgess, S., Davies, N. M., & Thompson, S. G. (2014). "Instrumental variable analysis with a nonlinear exposure–outcome relationship". Epidemiology (Cambridge, Mass.), 25(6), 877. (Residual stratification)

Tian, H., Mason, A. M., Liu, C., & Burgess, S. (2022). "Relaxing parametric assumptions for non-linear Mendelian randomization using a doubly-ranked stratification method". bioRxiv, 2022-06. (Doubly-ranked stratification)

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
odat<-res$traning.set #training set
vdat<-res$testing.set #testing set
GetIndex(odat,JJ=20)</pre>
```

getMSE	$Get \ MSE \ Value$	s for the OOB	Data or the	Testing Data with
	Fitted Q-Tree or	Random Fores	st of Q-Trees	(RFQT)

Description

getMSE calculates the MSE value for RFQT (or a Q-tree if RFQT only contains one single tree)

Usage

Arguments

RES	a fitting list result from BootstrapTreeFitting or RFQTfit(odat,vdat) RES
indicator	numeric indicator to judge which type of MSE should be calculated. indicator=1 for Out-of-Bag (OOB) data and indicator=2 for th testing data. Defalut value is indicator=1.

Value

getMSE returns a vector of MSE with the increase of the number of Q-trees. The stable MSE values should indicate an appropriate number of Q-trees.

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
res<-getDat(label=FALSE)
odat<-res$traning.set #training set</pre>
vdat<-res$testing.set #testing set
##When running RFQT with mutiple Q trees/bootstrap - use parallel computation
Nb<-7 #how many trees in the forest? e.g. 5 trees
cl<-makeCluster(2)</pre>
clusterEvalQ(cl=cl , expr=library(dplyr))
clusterEvalQ(cl=cl , expr=library(MendelianRandomization) )
clusterExport( cl=cl , varlist=c('odat','vdat',
                                     'GetTree', 'GetNindex', 'GetIndex' ) )
                cl , 1:Nb, BootstrapTreeFitting )
RES<-parSapply(
stopCluster(cl)
dim(RES)#7 Nb
getMSE(RES, indicator=1 )
getMSE(RES,indicator=2 )
```

 ${\tt GetNindex}$

Get the Q Tree End Node Index for Choosen Samples

Description

GetNindex helps to match the Q-tree end node for any inputed samples, and therefore enables to make further analysis like effect prediction for these inputed samples.

Usage

GetNindex(M, rdat, S = NA)

Arguments

М	A matrix or data frame contains the candidate covariate information.
rdat	A data frame. It is the Q-tree informaton result and obtained by ${\tt rdat <-GetTree()}.$
S	A positive integer indicates the max depth of each sample will explore along the tree. This number should be consistent with the max depth of the fitted Q tree (also refected in rdat). The default value if NA, which means the code will automatically use the correct S value.

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getPars

Details

The inputed data set M must contain the same candidate covariate information (with the same order) as the training data for the Q-tree. In addition, the first four columns (individual IDs, the instrument, the exposure, the outcome) need to be removed, so that the first column starts from the first candidate covariate.

Value

GetNindex returns a vector with the same length of the row number of the inputed data M. Each element represents the end node (i.e. leaf) index according to the reference Q-tree (the tree information was stored within rdat).

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
odat<-res$traning.set #training set</pre>
vdat<-res$testing.set #testing set
rdat<-GetTree(odat)
vdat_Nindex<-GetNindex(vdat[,5:24] ,rdat )</pre>
#the M colnumber and order should be same as the training data
#may use another independent data (estimation data) to
#calculate the endnode-specific IV/MR estimates
#for example:
#let odat halves into trdata (tree data) and estdata (estimation data);
#also we can have rdat<-GetTree(trdata)</pre>
trdat<-odat[1: (nrow(odat)/2) ,]#tree data</pre>
estdat<-odat[(nrow(odat)/2+1):nrow(odat) ,] #estimaiton data
rdat<-GetTree(trdat)#fitted Q tree</pre>
estdat$Nindex<-GetNindex(estdat[,5:24] ,rdat )</pre>
#rdat contains the tree information (i.e. decision rule)
```

getPars

Get the present parameters information

Description

getPars returns the information of the (hyper-)parameters relevant to the Q-tree and RFQT fitting.

Usage

```
getPars(empty.argument)
```

Arguments

empty.argument

No arguments are needed.

Value

getPars() returns the following information: the total number of candidate covariates, the training data size, the testing data siz, the stratification method, the size of pre-stratum (if applicable), the proportion of the covariates randomly considered in each node split, the maximal tree depth allowed, the way to calculate the instrument-exposure associations, the fixed instrument-exposure association level (if applicable), the minimal node size, the threshold value of the Q statistic.

If the variable is not defined, it will return 'Not defined' with a value in brackets representing the default value for this variable when fitting RFQT.

Note that only the variable defined in the global environment will be considered. Even if one defines these variables, the functions like BootstrapTreeFitting and RFQTfit will use the default value if (s)he does not modify the function arguments.

See the original paper for the details of each parameter information.

Author(s)

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Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
res<-getDat()
odat<-res$traning.set #training set
vdat<-res$testing.set #testing set
method<-'DR'; SoP<-20; rate<-2/5
getPars()</pre>
```

getPredict

Get predict effects for the OOB Data or the Testing Data with Fitted Random Forest of Q-Trees (RFQT)

Description

getPredict calculates the predicted individual treatment effect estimates for RFQT, either for the OOB data or the testing data.

Usage

Arguments

RES	a fitting list result from <code>BootstrapTreeFitting</code> or <code>RFQTfit(odat,vdat)</code> RES
indicator	numeric indicator to judge which type of predicted effect should be pre- sented. indicator=1 for Out-of-Bag (OOB) data and indicator=2 for th testing data. Defalut value is indicator=1.

Details

See the relevant part of the original paper for more details of how to predict an individual effect according to a fitted Q tree (therefore a RFQT).

Value

getPredict returns a matrix where the row corresponds to the sample size (either the OOB data or the testing data, depending on the indicator used) and the column corresponds to the number of Q-trees. Each column represents the individual predicted effects with the present number of Q trees.

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
res<-getDat(label=FALSE)
odat<-res$traning.set #training set
vdat<-res$testing.set #testing set
##When running RFQT with mutiple Q trees/bootstrap - use parallel computation</pre>
```

 ${\tt GetTree}$

Fit and Get a Q Tree

Description

GetTree fits a data and construct a Q-tree. The fitted data is directly used to build tree (so no bootstrap). The tree information will be stored but not cleaned for further analysis. You may need BootstrapTreeFitting rather than this function.

Usage

```
GetTree(dat,
    S = 5,
    Qthreshold = 3.84,
    rate = 1,
    SpecificM = NA,
    method = "DR",
    SoP = 10,
    howGX = "SpecificGX",
    Halve = FALSE,
    const = NA,
    endsize = 1000)
```

Arguments

dat	a data frame. This data (without any bootstrap) will be fitted to construct a Q-tree.
S	a postive integer indicates the maximum tree depth allowed. Default value is 5 (i.e. the data set is allowed to be splitted at most 5 times). S is also conneted to the argument endsize, both of which work in a similar way. One may only restrict one of them and leave another one be a flexible value (e.g. S=100 or endsize=0).

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Qthreshold	A positive value used as the threshold value for the Q statistic. Default value is 3.0.
rate	a value ranging from 0 to 1 indicates the proportion of the candidate covariates to be randomly cosidered in each split when construcing the Q-tree. When rate=1, it means all the candiate covariates will be considered.
SpecificM	a vector indicates the index of candidate variables that can be considered in spliiting. The default value is NA , which means all candidate variables are possible to be considered.
method	a character indicates the stratification method used for constructing a Q-tree. There are currently three methods: the Doubly-ranked method (method='DR'), the residual methods (method='Residual') and the naive method (recognized by any character except 'DR' and 'Residual'). The default method is 'DR'.
SoP	a postive integer (>=2) indicates the size of pre-straum. Only applicable for the doubly-ranked stratification. Default value is 10.
howGX	a character indicates the way to calculate the instrument-exposure associations. Two ways are currenly allowed: the instrument-exposure associations estimated seperately at each stratum (howGX='SpecificGX'), or use a fixed instrument-exposure association (howGX='const')
Halve	Logical. Indictes whether to split the node by half: half (i.e. 5:5). Default value is ${\sf FALSE}.$
const	a value indicates the fixed instrument-exposure association value used for constructing the Q-tree. Only applicable for <code>howGX='SpecificGX'</code> .
endsize	a positive integer value indicates the minimual size of the node of Q-tree allowed. One can also control the endsize via S.

Details

dat must be a data frame that can be regonized by the functions. The first four columns must be the individual IDs, the (one-dimensional) instrument, the exposure (should be NA if not available), and the outcome, respectively. The (high-dimensional) covariates are then follwing. Note that all the functions may be working with incorrect column ordering, but the results are misleading. DO make sure the column variable order is correct.

If simulated data is used, there should be a end column named as true_STE. That is, dat\$true_STE is not NULL.

Value

GetTree returns a data set with the same row dimension as the inputed data dat. The returned data is 'augmented' with tree information including the tree end node index, and the splitting information in each split.

References

Burgess, S., Davies, N. M., & Thompson, S. G. (2014). "Instrumental variable analysis with a nonlinear exposure–outcome relationship". Epidemiology (Cambridge, Mass.), 25(6), 877. (Residual stratification)

Tian, H., Mason, A. M., Liu, C., & Burgess, S. (2023). "Relaxing parametric assumptions for non-linear Mendelian randomization using a doubly-ranked stratification method". PLOS Genetics, 19(6), e1010823. (Doubly-ranked stratification)

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
res<-getDat()
odat<-res$traning.set #training set</pre>
```

tree_result<-GetTree(odat)</pre>

```
getVI
```

Get Varibale Importance Measurements with Fitted Q-Tree or Random Forest of Q-Trees (RFQT)

Description

getVI calculates the Varibale Importance (VI) measurements for a random forest of Q-trees (RFQT).

Usage

getVI(RES, VItype = 2

Arguments

RES	$a\ fitting\ list\ result\ from\ {\tt BootstrapTreeFitting\ or\ RFQTfit(odat,vdat)} \$
VItype	numeric indicator to judge which type of VI measurement should be calcu- lated. VItype=1 for the classical way with the known individual treatment effects (i.e. label) and VItype=2 for case that the individual treatment effects are unavailable (as in most real application). Defalut value is VItype=2.

Details

See the VI measurement part of the original paper for more detailed VI introduction and the algorithm.

Value

getVI returns a vector indicating the variable importance (VI) measurements for all the candidate covariates (with the same ordering of the candidate covariates to the original fitting data).

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RFQTfit

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
res<-getDat(label=FALSE)
odat<-res$traning.set #training set</pre>
vdat<-res$testing.set #testing set
##When running RFQT with mutiple Q trees/bootstrap - use parallel computation
Nb<-7 #how many trees in the forest? e.g. 5 trees
cl<-makeCluster(2)</pre>
clusterEvalQ(cl=cl , expr=library(dplyr))
clusterEvalQ(cl=cl , expr=library(MendelianRandomization) )
clusterExport( cl=cl , varlist=c('odat','vdat',
                                    'GetTree', 'GetNindex', 'GetIndex' ) )
                 cl , 1:Nb, BootstrapTreeFitting )
RES<-parSapply(
stopCluster(cl)
dim(RES)#7 Nb
getVI(RES,VItype=1 )
getVI(RES,VItype=2 )
```

RFQTfit

```
Fit a Random Forest of Q Trees (RFQT)
```

Description

RFQTfit fits a data set (the training data) by the random forest of Q trees (RFQT), and return the summary results.

Usage

```
RFQTfit(odat,
    vdat = NA,
    Nb = 5,
    S = 5,
    honest = FALSE,
    rate = 0.4,
    SingleM = FALSE,
    Qthreshold = 3.84,
    method = "DR",
    SoP = 10,
    howGX = "SpecificGX",
    Halve = FALSE,
```

```
endsize = 1000,
const = NA,
Cores = NA,
trackfile=NA
)
```

Arguments

	- data france. This is necessarily data that the invite of data and
odat	a data frame. This is recognized as the training data set.
vdat	a data frame. This is recognized as the testing or validation data set. The default value is NA, indicating that no testing data will be considered.
Nb	a positive integer indicates the number of bootstrap (i.e. the number of Q-trees)
S	a postive integer indicates the maximum tree depth allowed. Default value is 5 (i.e. the data set is allowed to be splitted at most 5 times). S is also conneted to the argument endsize, both of which work in a similar way. One may only restrict one of them and leave another one be a flexible value (e.g. S=100 or endsize=0).
honest	logical value indicates whether to use the honest estimation style or not. Default value is FALSE. When honest estimation is used, the tree construction and the leaf-specific estimates will be obtained in two seperate samples of the (boostrapped) training data.
rate	a value ranging from 0 to 1 indicates the proportion of the candidate covariates to be randomly cosidered in each split when construcing the Q-tree.
SingleM	logical value indicates whether to use one single covariate variable at all times. Default value is FALSE. If SingleM=TRUE, the covariate used are the best variable indicated by GetIndex.
Qthreshold	a positive value used as the threshold value for the Q statistic. Default value is 3.84. One can set Qthreshold=0 to ignore the Q-related stopping rule.
method	a character indicates the stratification method used for constructing a Q-tree. There are currently three methods: the Doubly-ranked method (method='DR'), the residual methods (method='Residual') and the naive method (recognized by any character except 'DR' and 'Residual'). The default method is 'DR'.
SoP	a postive integer (>=2) indicates the size of pre-straum. Only applicable for the doubly-ranked stratification. Default value is 10 .
howGX	a character indicates the way to calculate the instrument-exposure associations. Two ways are currenly allowed: the instrument-exposure associations estimated seperately at each stratum (howGX='SpecificGX'), or use a fixed instrument-exposure association (howGX='const').
Halve	logical. Indictes whether to split the node by half: half (i.e. 5:5). Default value is ${\sf FALSE}.$
endsize	a positive integer value indicates the minimual size of the node of Q-tree. S and endsize work in a similar way.

const	a value indicates the fixed instrument-exposure association value used for constructing the Q-tree. Only applicable for <code>howGX='SpecificGX'</code> .
Cores	a positive integer indicates the number of cores should be used when run- ning random forest in parallel. Default value is the number of CPU cores minus one. You can check the number of CPU cores via detectCores().
trackfile	the path string indicates the file to store the running information in par- allel.

Details

RFQTfit is an integrated function combining other functions, including GetTree, BootstrapTreeFitting, getPredict, getVI, etc. The fitting automatically uses parallel computation.

The training data Odat and the testing data Vdat should be of the same form and be a data frame that can be regonized by the functions. The first four columns must be the individual IDs, the (one-dimensional) instrument, the exposure (should be NA if not available), and the outcome, respectively. The (high-dimensional) covariates are then following. Note that all the functions may be working with incorrect column ordering, but the results are misleading. DO make sure the column variable order is correct.

Value

RFQTfit shows all the parameter information used for random forest fitting in the beginnig, and returns in the end a list consisting of the following components:

RES	The direct fitting results of each Q-tree, which contains end_node_information, OOB_predict, v_predict, vi1, vi2, ts1 and ts2 (same as the results of BootstrapTreeFitting) for each Q-tree. Note that RES is multi-dimensional. If one wishes to obtain the individual predicted effects of the testing set according to i-th Q-tree, should run RES[3,i]\$v_predict.
MSE_OOB	the Nb-length vector of MSE results for OOB samples. If one determine the number of Q-trees to be Nb, simply use the final vlue of MSE_OOB as the MSE.
MSE_test	the Nb-length vector of MSE results for test samples (if the testing set exists). If one determine the number of Q-trees to be Nb, simply use the final vlue of MSE_test as the MSE.
Predict_00B	the matrix of predicted effects for OOB samples, where the row corre- sponds to the sample size (the testing data) and the column coresponds to the number of Q-trees. Each column represents the individual pre- dicted effects with the present number of Q trees. If one determine the number of Q-trees to be Nb, simply use the final column of Predict_OOB as the individual predicted effect vector.
Predict_test	the matrix of predicted effects for testing set, where the row corresponds to the sample size (the testing data) and the column corresponds to the number of Q-trees. Each column represents the individual predicted ef- fects with the present number of Q trees. If one determine the number of Q-trees to be Nb, simply use the final column of Predict_test as the individual predicted effect vector.

VI1	the vector indicates the type I (i.e. with labels) variable importance (VI) measurements for all the candidate covariates (with the same ordering of the candidate covariates to the original fitting data).
VI2	the vector indicates the type II (i.e. without labels) variable importance (VI) measurements for all the candidate covariates (with the same ordering of the candidate covariates to the original fitting data).
TS	the vector of the permutation test statistic values. The two values repre- sent the values of TS1 and TS2, respectively.

References

Burgess, S., Davies, N. M., & Thompson, S. G. (2014). "Instrumental variable analysis with a nonlinear exposure–outcome relationship". Epidemiology (Cambridge, Mass.), 25(6), 877. (Residual stratification)

Tian, H., Mason, A. M., Liu, C., & Burgess, S. (2023). "Relaxing parametric assumptions for non-linear Mendelian randomization using a doubly-ranked stratification method". PLOS Genetics, 19(6), e1010823. (Doubly-ranked stratification)

Examples

```
library(MendelianRandomization)
library(tidyverse)
library(data.table)
library(parallel)
```

```
set.seed(60)
res<-getDat() #simulated data #the deflaut setting: scenario='A' and SoM=0.5
odat<-res$traning.set
vdat<-res$testing.set</pre>
```

```
###try: ALLRES<-RFQTfit(odat)</pre>
```

###try: ALLRES<-RFQTfit(odat,vdat,Nb=200)</pre>

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